# Package 'GeneSelectMMD'

October 14, 2021

Type Package  Title Gene selection based on the marginal distributions of gene profiles that characterized by a mixture of three-component multivariate distributions  Version 2.36.0  Date 2020-04-03  Author Jarrett Morrow <remdj@channing.harvard.edu>, Weiliang Qiu <meiliang.qiu@gmail.com>, Wenqing He <meelstats.uwo.ca>, Xiaogang Wang <stevenw@mathstat.yorku.ca>, Ross Lazarus <ross.lazarus@channing.harvard.edu>.  Maintainer Weiliang Qiu <meiliang.qiu@gmail.com> Depends R (&gt;= 2.13.2), Biobase  Imports MASS, graphics, stats, limma  Suggests ALL  Description Gene selection based on a mixture of marginal distributions.  License GPL (&gt;= 2) bioeViews DifferentialExpression git_url https://git.bioconductor.org/packages/GeneSelectMMD git_branch RELEASE_3_13 git_last_commit_c1e5d5d git_last_commit_date 2021-05-19  Date/Publication 2021-10-14  R topics documented:  crrRates</meiliang.qiu@gmail.com></ross.lazarus@channing.harvard.edu></stevenw@mathstat.yorku.ca></meelstats.uwo.ca></meiliang.qiu@gmail.com></remdj@channing.harvard.edu>		
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## **Description**

Calculating FDR, FNDR, FPR, and FNR for a real microarray data set based on the mixture of marginal distributions.

## Usage

```
errRates(obj.gsMMD)
```

## **Arguments**

obj.gsMMD an object returned by gsMMD.gsMMD.default, gsMMD2, or gsMMD2.default

### **Details**

We first fit the real microarray data set by the mixture of marginal distributions. Then we calculate the error rates based on the posterior distributions of a gene belonging to a gene cluster given its gene profiles. Please refer to Formula (7) on the page 6 of the paper listed in the Reference section.

## Value

A vector of 4 elements:

FDR	the percentage of nondifferentially expressed genes among selected genes.
FNDR	the percentage of differentially expressed genes among unselected genes.
FPR	the percentage of selected genes among nondifferentially expressed genes
FNR	the percentage of un-selected genes among differentially expressed genes

## Author(s)

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#### References

Qiu, W.-L., He, W., Wang, X.-G. and Lazarus, R. (2008). A Marginal Mixture Model for Selecting Differentially Expressed Genes across Two Types of Tissue Samples. *The International Journal of Biostatistics*. 4(1):Article 20. http://www.bepress.com/ijb/vol4/iss1/20

## **Examples**

```
## Not run:
   library(ALL)
   data(ALL)
   eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]

mem.str <- as.character(eSet1$BT)
   nSubjects <- length(mem.str)
   memSubjects <- rep(0,nSubjects)
   # B3 coded as 0, T2 coded as 1
   memSubjects[mem.str == "T2"] <- 1

obj.gsMMD <- gsMMD(eSet1, memSubjects, transformFlag = TRUE,
        transformMethod = "boxcox", scaleFlag = TRUE, quiet = FALSE)
   round(errRates(obj.gsMMD), 3)

## End(Not run)</pre>
```

gsMMD

Gene selection based on a mixture of marginal distributions

## **Description**

Gene selection based on the marginal distributions of gene profiles that characterized by a mixture of three-component multivariate distributions. Input is an object derived from the class ExpressionSet. The function will obtain initial gene cluster membership by its own.

## Usage

```
gsMMD(obj.eSet,
      memSubjects,
      maxFlag = TRUE,
      thrshPostProb = 0.5,
      geneNames = NULL,
      alpha = 0.05,
      iniGeneMethod = "Ttest",
      transformFlag = FALSE,
      transformMethod = "boxcox",
      scaleFlag = TRUE,
      criterion = c("cor", "skewness", "kurtosis"),
      minL = -10,
      maxL = 10,
      stepL = 0.1,
      eps = 0.001,
      ITMAX = 100,
      plotFlag = FALSE,
      quiet=TRUE)
```

#### **Arguments**

obj.eSet an object derived from the class ExpressionSet which contains the matrix of

gene expression levels. The rows of the matrix are genes. The columns of the

matrix are subjects.

memSubjects a vector of membership of subjects. memSubjects[i]=1 means the i-th subject

belongs to diseased group, 0 otherwise.

maxFlag logical. Indicate how to assign gene class membership. maxFlag=TRUE means

that a gene will be assigned to a class in which the posterior probability of the gene belongs to this class is maximum. maxFlag=FALSE means that a gene will be assigned to class 1 if the posterior probability of the gene belongs to class 1 is greater than thrshPostProb. Similarly, a gene will be assigned to class 1 if the posterior probability of the gene belongs to class 1 is greater than thrshPostProb. If the posterior probability is less than thrshPostProb, the

gene will be assigned to class 2 (non-differentially expressed gene group).

thrshPostProb threshold for posterior probabilities. For example, if the posterior probability

that a gene belongs to cluster 1 given its gene expression levels is larger than

thrshPostProb, then this gene will be assigned to cluster 1.

geneNames an optional character vector of gene names

alpha significant level which is equal to 1-conf.level, conf.level is the argument

for the function t.test.

iniGeneMethod method to get initial 3-cluster partition of genes. Available methods are: "Ttest",

"Wilcox".

transformFlag logical. Indicate if data transformation is needed

transformMethod

method for transforming data. Available methods include "boxcox", "log2",

"log10", "log", "none".

scaleFlag logical. Indicate if gene profiles are to be scaled to have mean zero and variance

one. If transformFlag=TRUE and scaleFlag=TRUE, then scaling is performed after transformation. To avoid linear dependence of tissue samples after scaling

gene profiles, we delete one tissue sample after scaling (c.f. details).

criterion if transformFlag=TRUE, criterion indicates what criterion to determine if

data looks like normal. "cor" means using Pearson's correlation. The idea is that the observed quantiles after transformation should be close to theoretical normal quantiles. So we can use Pearson's correlation to check if the scatter plot of theoretical normal quantiles versus observed quantiles is a straightline. "skewness" means using skewness measure to check if the distribution of the transformed data are close to normal distribution; "kurtosis" means using kurto-

sis measure to check normality.

minL lower limit for the lambda parameter used in Box-Cox transformation upper limit for the lambda parameter used in Box-Cox transformation

stepL tolerance when searching the optimal lambda parameter used in Box-Cox trans-

formation

eps a small positive value. If the absolute value of a value is smaller than eps, this

value is regarded as zero.

ITMAX maximum iteration allowed for iterations in the EM algorithm

plotFlag logical. Indicate if the Box-Cox normality plot should be output.

quiet logical. Indicate if intermediate results should be printed out.

#### **Details**

We assume that the distribution of gene expression profiles is a mixture of 3-component multivariate normal distributions  $\sum_{k=1}^3 \pi_k f_k(x|\theta)$ . Each component distribution  $f_k$  corresponds to a gene cluster. The 3 components correspond to 3 gene clusters: (1) up-regulated gene cluster, (2) non-differentially expressed gene cluster, and (3) down-regulated gene cluster. The model parameter vector is  $\theta = (\pi_1, \pi_2, \pi_3, \mu_{c1}, \sigma_{c1}^2, \rho_{c1}, \mu_{n1}, \sigma_{n1}^2, \rho_{n1}, \mu_2, \sigma_2^2, \rho_2, \mu_{c3}, \sigma_{c3}^2, \rho_{c3}, \mu_{n3}, \sigma_{n3}^2, \rho_{n3}$ . where  $\pi_1, \pi_2$ , and  $\pi_3$  are the mixing proportions;  $\mu_{c1}, \sigma_{c1}^2$ , and  $\rho_{c1}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 1 (up-regulated genes) for diseased subjects;  $\mu_{n1}, \sigma_{n1}^2$ , and  $\rho_{n1}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 1 (up-regulated genes) for non-diseased subjects;  $\mu_2, \sigma_2^2$ , and  $\rho_2$  are the marginal mean, variance, and correlation of gene expression levels of cluster 2 (non-differentially expressed genes);  $\mu_{c3}, \sigma_{c3}^2$ , and  $\rho_{c3}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for diseased subjects;  $\mu_{n3}, \sigma_{n3}^2$ , and  $\rho_{n3}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for non-diseased subjects.

Note that genes in cluster 2 are non-differentially expressed across abnormal and normal tissue samples. Hence there are only 3 parameters for cluster 2.

To make sure the identifiability, we set the following contraints:  $\mu_{c1} > \mu_{n1}$  and  $\mu_{c3} < \mu_{n3}$ .

To make sure the marginal covariance matrices are poisitive definite, we set the following contraints:  $-1/(n_c-1) < \rho_{c1} < 1, -1/(n_n-1) < \rho_{n1} < 1, -1/(n-1) < \rho_2 < 1, -1/(n_c-1) < \rho_{c3} < 1, -1/(n_n-1) < \rho_{n3} < 1.$ 

We also has the following constraints for the mixing proportion:  $\pi_3 = 1 - \pi_1 - \pi_2$ ,  $\pi_k > 0$ , k = 1, 2, 3.

We apply the EM algorithm to estimate the model parameters. We regard the cluster membership of genes as missing values.

To facilitate the estimation of the parameters, we reparametrize the parameter vector as  $\theta^* = (\pi_1, \pi_2, \mu_{c1}, \sigma_{c1}^2, r_{c1}, \delta_{n1}, \sigma_{n1}^2, r_{n1}, \mu_2, \sigma_2^2, r_2, \mu_{c3}, \sigma_{c3}^2, r_{c3}, \delta_{n3}, \sigma_{n3}^2, r_{n3})$ , where  $\mu_{n1} = \mu_{c1} - \exp(\delta_{n1}), \mu_{n3} = \mu_{c3} + \exp(\delta_{n3}), \rho_{c1} = (\exp(r_{c1}) - 1/(n_c - 1))/(1 + \exp(r_{c1})), \rho_{n1} = (\exp(r_{n1}) - 1/(n_n - 1))/(1 + \exp(r_{n1})), \rho_{2} = (\exp(r_2) - 1/(n_c - 1))/(1 + \exp(r_2)), \rho_{c3} = (\exp(r_{c3}) - 1/(n_c - 1))/(1 + \exp(r_{c3})), \rho_{n3} = (\exp(r_{n3}) - 1/(n_n - 1))/(1 + \exp(r_{n3})).$ 

Given a gene, the expression levels of the gene are assumed independent. However, after scaling, the scaled expression levels of the gene are no longer independent and the rank  $r^* = r - 1$  of the covariance matrix for the scaled gene profile will be one less than the rank r for the un-scaled gene profile Hence the covariance matrix of the gene profile will no longer be positive-definite. To avoid this problem, we delete a tissue sample after scaling since its information has been incorrporated by other scaled tissue samples. We arbitrarily select the tissue sample, which has the biggest label number, from the tissue sample group that has larger size than the other tissue sample group. For example, if there are 6 cancer tissue samples and 10 normal tissue samples, we delete the 10-th normal tissue sample after scaling.

#### Value

A list contains 18 elements.

dat the (transformed) microarray data matrix. If transformation performed, then dat

will be different from the input microarray data matrix.

memSubjects the same as the input memSubjects.

memGenes a vector of cluster membership of genes. 1 means up-regulated gene; 2 means

non-differentially expressed gene; 3 means down-regulated gene.

memGenes2 an variant of the vector of cluster membership of genes. 1 means differentially

expressed gene; 0 means non-differentially expressed gene.

para parameter estimates (c.f. details).

11kh value of the loglikelihood function.

wiMat posterior probability that a gene belongs to a cluster given the expression levels

of this gene. Column i is for cluster i.

wiArray posterior probability matrix for different initial gene selection methods.

memIniMat a matrix of initial cluster membership of genes.

paraIniMat a matrix of parameter estimates based on initial gene cluster membership.

11khIniVec a vector of values of loglikelihood function.

memMat a matrix of cluster membership of genes based on the mixture of marginal mod-

els with initial parameter estimates obtained initial gene cluster membership.

paraMat a matrix of parameter estimates based on the mixture of marginal models with

initial parameter estimates obtained initial gene cluster membership.

11khVec a vector of values of loglikelihood function based on the mixture of marginal

models with initial parameter estimates obtained initial gene cluster member-

ship.

lambda the parameter used to do Box-Cox transformation

parameter estimates for reparametrized parameter vector (c.f. details).

paraIniMatRP a matrix of parameter estimates for reparametrized parameter vector based on

initial gene cluster membership.

paraMatRP a matrix of parameter estimates for reparametrized parameter vector based on

the mixture of marginal models with initial parameter estimates obtained initial

gene cluster membership.

#### Note

The speed of the program can be slow for large data sets, however it has been improved using Fortran code.

#### Author(s)

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### References

Qiu, W.-L., He, W., Wang, X.-G. and Lazarus, R. (2008). A Marginal Mixture Model for Selecting Differentially Expressed Genes across Two Types of Tissue Samples. *The International Journal of Biostatistics*. 4(1):Article 20. http://www.bepress.com/ijb/vol4/iss1/20

#### See Also

```
gsMMD.default, gsMMD2, gsMMD2.default
```

## **Examples**

```
library(ALL)
data(ALL)
eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]

mem.str <- as.character(eSet1$BT)
nSubjects <- length(mem.str)
memSubjects <- rep(0,nSubjects)
# B3 coded as 0, T2 coded as 1
memSubjects[mem.str == "T2"] <- 1

obj.gsMMD <- gsMMD(eSet1, memSubjects, transformFlag = TRUE,
    transformMethod = "boxcox", scaleFlag = TRUE, quiet = FALSE)
round(obj.gsMMD$para, 3)</pre>
```

gsMMD.default

Gene selection based on a mixture of marginal distributions

## **Description**

Gene selection based on the marginal distributions of gene profiles that characterized by a mixture of three-component multivariate distributions. Input is a data matrix. The function will obtain initial gene cluster membership by its own.

## Usage

```
maxL = 10,
stepL = 0.1,
eps = 0.001,
ITMAX = 100,
plotFlag = FALSE,
quiet=TRUE)
```

#### **Arguments**

X a data matrix. The rows of the matrix are genes. The columns of the matrix are

subjects.

memSubjects a vector of membership of subjects. memSubjects[i]=1 means the i-th subject

belongs to diseased group, 0 otherwise.

maxFlag logical. Indicate how to assign gene class membership. maxFlag=TRUE means

that a gene will be assigned to a class in which the posterior probability of the gene belongs to this class is maximum. maxFlag=FALSE means that a gene will be assigned to class 1 if the posterior probability of the gene belongs to class 1 is greater than thrshPostProb. Similarly, a gene will be assigned to class 1 if the posterior probability of the gene belongs to class 1 is greater than thrshPostProb. If the posterior probability is less than thrshPostProb, the

gene will be assigned to class 2 (non-differentially expressed gene group).

thrshPostProb threshold for posterior probabilities. For example, if the posterior probability

that a gene belongs to cluster 1 given its gene expression levels is larger than

thrshPostProb, then this gene will be assigned to cluster 1.

geneNames an optional character vector of gene names

alpha significant level which is equal to 1-conf.level, conf.level is the argument

for the function t.test.

iniGeneMethod method to get initial 3-cluster partition of genes. Available methods are: "Ttest",

"Wilcox".

transformFlag logical. Indicate if data transformation is needed

transformMethod

method for transforming data. Available methods include "boxcox", "log2",

"log10", "log", "none".

scaleFlag logical. Indicate if gene profiles are to be scaled. If transformFlag=TRUE and

scaleFlag=TRUE, then scaling is performed after transformation. To avoid linear dependence of tissue samples after scaling gene profiles, we delete one tissue

sample after scaling (c.f. details).

criterion if transformFlag=TRUE, criterion indicates what criterion to determine if

data looks like normal. "cor" means using Pearson's correlation. The idea is that the observed quantiles after transformation should be close to theoretical normal quantiles. So we can use Pearson's correlation to check if the scatter plot of theoretical normal quantiles versus observed quantiles is a straightline. "skewness" means using skewness measure to check if the distribution of the transformed data are close to normal distribution; "kurtosis" means using kurto-

sis measure to check normality.

minL lower limit for the lambda parameter used in Box-Cox transformation

maxL	upper limit for the lambda parameter used in Box-Cox transformation
stepL	tolerance when searching the optimal lambda parameter used in Box-Cox transformation $% \left( 1\right) =\left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left$
eps	a small positive value. If the absolute value of a value is smaller than eps, this value is regarded as zero.
ITMAX	maximum iteration allowed for iterations in the EM algorithm
plotFlag	logical. Indicate if the Box-Cox normality plot should be output.
quiet	logical. Indicate if intermediate results should be printed out.

#### **Details**

We assume that the distribution of gene expression profiles is a mixture of 3-component multivariate normal distributions  $\sum_{k=1}^3 \pi_k f_k(x|\theta)$ . Each component distribution  $f_k$  corresponds to a gene cluster. The 3 components correspond to 3 gene clusters: (1) up-regulated gene cluster, (2) non-differentially expressed gene cluster, and (3) down-regulated gene cluster. The model parameter vector is  $\theta = (\pi_1, \pi_2, \pi_3, \mu_{c1}, \sigma_{c1}^2, \rho_{c1}, \mu_{n1}, \sigma_{n1}^2, \rho_{n1}, \mu_2, \sigma_2^2, \rho_2, \mu_{c3}, \sigma_{c3}^2, \rho_{c3}, \mu_{n3}, \sigma_{n3}^2, \rho_{n3}$ . where  $\pi_1, \pi_2$ , and  $\pi_3$  are the mixing proportions;  $\mu_{c1}, \sigma_{c1}^2$ , and  $\rho_{c1}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 1 (up-regulated genes) for diseased subjects;  $\mu_{n1}, \sigma_{n1}^2$ , and  $\rho_{n1}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 1 (up-regulated genes) for non-diseased subjects;  $\mu_2, \sigma_2^2$ , and  $\rho_2$  are the marginal mean, variance, and correlation of gene expression levels of cluster 2 (non-differentially expressed genes);  $\mu_{c3}, \sigma_{c3}^2$ , and  $\rho_{c3}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for diseased subjects;  $\mu_{n3}, \sigma_{n3}^2$ , and  $\rho_{n3}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for non-diseased subjects;  $\mu_{n3}, \sigma_{n3}^2$ , and  $\rho_{n3}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for non-diseased subjects;  $\mu_{n3}, \sigma_{n3}^2$ , and  $\rho_{n3}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for non-diseased subjects.

Note that genes in cluster 2 are non-differentially expressed across abnormal and normal tissue samples. Hence there are only 3 parameters for cluster 2.

To make sure the identifiability, we set the following contraints:  $\mu_{c1} > \mu_{n1}$  and  $\mu_{c3} < \mu_{n3}$ .

To make sure the marginal covariance matrices are poisitive definite, we set the following contraints:  $-1/(n_c-1) < \rho_{c1} < 1, -1/(n_n-1) < \rho_{n1} < 1, -1/(n-1) < \rho_2 < 1, -1/(n_c-1) < \rho_{c3} < 1, -1/(n_n-1) < \rho_{n3} < 1.$ 

We also has the following constraints for the mixing proportion:  $\pi_3 = 1 - \pi_1 - \pi_2$ ,  $\pi_k > 0$ , k = 1, 2, 3.

We apply the EM algorithm to estimate the model parameters. We regard the cluster membership of genes as missing values.

To facilitate the estimation of the parameters, we reparametrize the parameter vector as  $\theta^* = (\pi_1, \pi_2, \mu_{c1}, \sigma_{c1}^2, r_{c1}, \delta_{n1}, \sigma_{n1}^2, r_{n1}, \mu_2, \sigma_2^2, r_2, \mu_{c3}, \sigma_{c3}^2, r_{c3}, \delta_{n3}, \sigma_{n3}^2, r_{n3})$ , where  $\mu_{n1} = \mu_{c1} - \exp(\delta_{n1}), \mu_{n3} = \mu_{c3} + \exp(\delta_{n3}), \rho_{c1} = (\exp(r_{c1}) - 1/(n_c - 1))/(1 + \exp(r_{c1})), \rho_{n1} = (\exp(r_{n1}) - 1/(n_n - 1))/(1 + \exp(r_{n1})), \rho_{2} = (\exp(r_2) - 1/(n_c - 1))/(1 + \exp(r_2)), \rho_{c3} = (\exp(r_{c3}) - 1/(n_c - 1))/(1 + \exp(r_{c3})), \rho_{n3} = (\exp(r_{n3}) - 1/(n_n - 1))/(1 + \exp(r_{n3})).$ 

Given a gene, the expression levels of the gene are assumed independent. However, after scaling, the scaled expression levels of the gene are no longer independent and the rank  $r^* = r - 1$  of the covariance matrix for the scaled gene profile will be one less than the rank r for the un-scaled gene profile Hence the covariance matrix of the gene profile will no longer be positive-definite. To avoid this problem, we delete a tissue sample after scaling since its information has been incorrporated

by other scaled tissue samples. We arbitrarily select the tissue sample, which has the biggest label number, from the tissue sample group that has larger size than the other tissue sample group. For example, if there are 6 cancer tissue samples and 10 normal tissue samples, we delete the 10-th normal tissue sample after scaling.

#### Value

A list contains 18 elements.

dat the (transformed) microarray data matrix. If tranformation performed, then dat

will be different from the input microarray data matrix.

memSubjects the same as the input memSubjects.

memGenes a vector of cluster membership of genes. 1 means up-regulated gene; 2 means

non-differentially expressed gene; 3 means down-regulated gene.

memGenes2 an variant of the vector of cluster membership of genes. 1 means differentially

expressed gene; 0 means non-differentially expressed gene.

para parameter estimates (c.f. details).

11kh value of the loglikelihood function.

wiMat posterior probability that a gene belongs to a cluster given the expression levels

of this gene. Column i is for cluster i.

wiArray posterior probability matrix for different initial gene selection methods.

memIniMat a matrix of initial cluster membership of genes.

paraIniMat a matrix of parameter estimates based on initial gene cluster membership.

11khIniVec a vector of values of loglikelihood function.

memMat a matrix of cluster membership of genes based on the mixture of marginal mod-

els with initial parameter estimates obtained initial gene cluster membership.

paraMat a matrix of parameter estimates based on the mixture of marginal models with

initial parameter estimates obtained initial gene cluster membership.

11khVec a vector of values of loglikelihood function based on the mixture of marginal

models with initial parameter estimates obtained initial gene cluster member-

ship.

lambda the parameter used to do Box-Cox transformation

parameter estimates for reparametrized parameter vector (c.f. details).

paraIniMatRP a matrix of parameter estimates for reparametrized parameter vector based on

initial gene cluster membership.

paraMatRP a matrix of parameter estimates for reparametrized parameter vector based on

the mixture of marginal models with initial parameter estimates obtained initial

gene cluster membership.

## Note

The speed of the program can be slow for large data sets, however it has been improved using Fortran code.

#### Author(s)

Jarrett Morrow <remdj@channing.harvard.edu>, Weiliang Qiu <Weiliang.Qiu@gmail.com>, Wenqing He <whe@stats.uwo.ca>, Xiaogang Wang <stevenw@mathstat.yorku.ca>, Ross Lazarus <ross.lazarus@channing.harvard.edu>

#### References

Qiu, W.-L., He, W., Wang, X.-G. and Lazarus, R. (2008). A Marginal Mixture Model for Selecting Differentially Expressed Genes across Two Types of Tissue Samples. *The International Journal of Biostatistics*. 4(1):Article 20. http://www.bepress.com/ijb/vol4/iss1/20

#### See Also

```
gsMMD, gsMMD2, gsMMD2.default
```

## **Examples**

gsMMD2

Gene selection based on a mixture of marginal distributions

## **Description**

Gene selection based on the marginal distributions of gene profiles that characterized by a mixture of three-component multivariate distributions. Input is an object derived from the class ExpressionSet. The user needs to provide initial gene cluster membership.

### Usage

```
gsMMD2(obj.eSet,
       memSubjects,
       memIni,
       maxFlag = TRUE,
       thrshPostProb = 0.5,
       geneNames = NULL,
       alpha = 0.05,
       transformFlag = FALSE,
       transformMethod = "boxcox",
       scaleFlag = TRUE,
       criterion = c("cor", "skewness", "kurtosis"),
       minL = -10,
       maxL = 10,
       stepL = 0.1,
       eps = 0.001,
       ITMAX = 100,
       plotFlag = FALSE,
       quiet=TRUE)
```

#### **Arguments**

obj.eSet an object derived from the class ExpressionSet which contains the matrix of

gene expression levels. The rows of the matrix are genes. The columns of the

matrix are subjects.

memSubjects a vector of membership of subjects. memSubjects[i]=1 means that the i-th

subject belongs to diseased group, 0 otherwise.

memIni a vector of user-provided gene cluster membership.

maxFlag logical. Indicate how to assign gene class membership. maxFlag=TRUE means

that a gene will be assigned to a class in which the posterior probability of the gene belongs to this class is maximum. maxFlag=FALSE means that a gene will be assigned to class 1 if the posterior probability of the gene belongs to class 1 is greater than thrshPostProb. Similarly, a gene will be assigned to class 1 if the posterior probability of the gene belongs to class 1 is greater than thrshPostProb. If the posterior probability is less than thrshPostProb, the

gene will be assigned to class 2 (non-differentially expressed gene group).

thrshPostProb threshold for posterior probabilities. For example, if the posterior probability

that a gene belongs to cluster 1 given its gene expression levels is larger than

thrshPostProb, then this gene will be assigned to cluster 1.

geneNames an optional character vector of gene names

alpha significant level which is equal to 1-conf.level, conf.level is the argument

for the function t.test.

transformFlag logical. Indicate if data transformation is needed

transformMethod

method for transforming data. Available methods include "boxcox", "log2",

"log10", "log", "none".

scaleFlag logical. Indicate if gene profiles are to be scaled. If transformFlag=TRUE and scaleFlag=TRUE, then scaling is performed after transformation. To avoid linear dependence of tissue samples after scaling gene profiles, we delete one tissue sample after scaling (c.f. details).

if transformFlag=TRUE, criterion indicates what criterion to determine if

data looks like normal. "cor" means using Pearson's correlation. The idea is that the observed quantiles after transformation should be close to theoretical normal quantiles. So we can use Pearson's correlation to check if the scatter plot of theoretical normal quantiles versus observed quantiles is a straightline. "skewness" means using skewness measure to check if the distribution of the transformed data are close to normal distribution; "kurtosis" means using kurto-

sis measure to check normality.

minL lower limit for the lambda parameter used in Box-Cox transformation maxL upper limit for the lambda parameter used in Box-Cox transformation

stepL tolerance when searching the optimal lambda parameter used in Box-Cox trans-

formation

eps a small positive value. If the absolute value of a value is smaller than eps, this

value is regarded as zero.

ITMAX maximum iteration allowed for iterations in the EM algorithm plotFlag logical. Indicate if the Box-Cox normality plot should be output. logical. Indicate if intermediate results should be printed out.

#### **Details**

criterion

We assume that the distribution of gene expression profiles is a mixture of 3-component multivariate normal distributions  $\sum_{k=1}^3 \pi_k f_k(x|\theta)$ . Each component distribution  $f_k$  corresponds to a gene cluster. The 3 components correspond to 3 gene clusters: (1) up-regulated gene cluster, (2) non-differentially expressed gene cluster, and (3) down-regulated gene cluster. The model parameter vector is  $\theta = (\pi_1, \pi_2, \pi_3, \mu_{c1}, \sigma_{c1}^2, \rho_{c1}, \mu_{n1}, \sigma_{n1}^2, \rho_{n1}, \mu_2, \sigma_2^2, \rho_2, \mu_{c3}, \sigma_{c3}^2, \rho_{c3}, \mu_{n3}, \sigma_{n3}^2, \rho_{n3}$ . where  $\pi_1, \pi_2$ , and  $\pi_3$  are the mixing proportions;  $\mu_{c1}, \sigma_{c1}^2$ , and  $\rho_{c1}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 1 (up-regulated genes) for diseased subjects;  $\mu_{n1}, \sigma_{n1}^2$ , and  $\rho_{n1}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 1 (up-regulated genes) for non-diseased subjects;  $\mu_2, \sigma_2^2$ , and  $\rho_2$  are the marginal mean, variance, and correlation of gene expression levels of cluster 2 (non-differentially expressed genes);  $\mu_{c3}, \sigma_{c3}^2$ , and  $\rho_{c3}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for diseased subjects;  $\mu_{n3}, \sigma_{n3}^2$ , and  $\rho_{n3}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for non-diseased subjects.

Note that genes in cluster 2 are non-differentially expressed across abnormal and normal tissue samples. Hence there are only 3 parameters for cluster 2.

To make sure the identifiability, we set the following contraints:  $\mu_{c1} > \mu_{n1}$  and  $\mu_{c3} < \mu_{n3}$ .

To make sure the marginal covariance matrices are poisitive definite, we set the following contraints:  $-1/(n_c-1) < \rho_{c1} < 1, -1/(n_n-1) < \rho_{n1} < 1, -1/(n-1) < \rho_2 < 1, -1/(n_c-1) < \rho_{c3} < 1, -1/(n_n-1) < \rho_{n3} < 1.$ 

We also has the following constraints for the mixing proportion:  $\pi_3 = 1 - \pi_1 - \pi_2$ ,  $\pi_k > 0$ , k = 1, 2, 3.

We apply the EM algorithm to estimate the model parameters. We regard the cluster membership of genes as missing values.

To facilitate the estimation of the parameters, we reparametrize the parameter vector as  $\theta^* = (\pi_1, \pi_2, \mu_{c1}, \sigma_{c1}^2, r_{c1}, \delta_{n1}, \sigma_{n1}^2, r_{n1}, \mu_2, \sigma_2^2, r_2, \mu_{c3}, \sigma_{c3}^2, r_{c3}, \delta_{n3}, \sigma_{n3}^2, r_{n3})$ , where  $\mu_{n1} = \mu_{c1} - \exp(\delta_{n1}), \mu_{n3} = \mu_{c3} + \exp(\delta_{n3}), \rho_{c1} = (\exp(r_{c1}) - 1/(n_c - 1))/(1 + \exp(r_{c1})), \rho_{n1} = (\exp(r_{n1}) - 1/(n_n - 1))/(1 + \exp(r_{n1})), \rho_{2} = (\exp(r_2) - 1/(n_c - 1))/(1 + \exp(r_2)), \rho_{c3} = (\exp(r_{c3}) - 1/(n_c - 1))/(1 + \exp(r_{c3})), \rho_{n3} = (\exp(r_{n3}) - 1/(n_n - 1))/(1 + \exp(r_{n3})).$ 

Given a gene, the expression levels of the gene are assumed independent. However, after scaling, the scaled expression levels of the gene are no longer independent and the rank  $r^* = r - 1$  of the covariance matrix for the scaled gene profile will be one less than the rank r for the un-scaled gene profile Hence the covariance matrix of the gene profile will no longer be positive-definite. To avoid this problem, we delete a tissue sample after scaling since its information has been incorrporated by other scaled tissue samples. We arbitrarily select the tissue sample, which has the biggest label number, from the tissue sample group that has larger size than the other tissue sample group. For example, if there are 6 cancer tissue samples and 10 normal tissue samples, we delete the 10-th normal tissue sample after scaling.

#### Value

A list contains 13 elements.

dat the (transformed) microarray data matrix. If transformation performed, then dat

will be different from the input microarray data matrix.

memSubjects the same as the input memSubjects.

memGenes a vector of cluster membership of genes. 1 means up-regulated gene; 2 means

non-differentially expressed gene; 3 means down-regulated gene.

memGenes2 an variant of the vector of cluster membership of genes. 1 means differentially

expressed gene; 0 means non-differentially expressed gene.

para parameter estimates (c.f. details).

11kh value of the loglikelihood function.

wiMat posterior probability that a gene belongs to a cluster given the expression levels

of this gene. Column i is for cluster i.

memIni the initial cluster membership of genes.

paraIni the parameter estimates based on initial gene cluster membership.

11khIni the value of loglikelihood function.

lambda the parameter used to do Box-Cox transformation

parameter estimates for reparametrized parameter vector (c.f. details).

paraIniRP the parameter estimates for reparametrized parameter vector based on initial

gene cluster membership.

## Note

The speed of the program can be slow for large data sets, however it has been improved using Fortran code.

#### Author(s)

Jarrett Morrow <remdj@channing.harvard.edu>, Weiliang Qiu <Weiliang.Qiu@gmail.com>, Wenqing He <whe@stats.uwo.ca>, Xiaogang Wang <stevenw@mathstat.yorku.ca>, Ross Lazarus <ross.lazarus@channing.harvard.edu>

#### References

Qiu, W.-L., He, W., Wang, X.-G. and Lazarus, R. (2008). A Marginal Mixture Model for Selecting Differentially Expressed Genes across Two Types of Tissue Samples. *The International Journal of Biostatistics*. 4(1):Article 20. http://www.bepress.com/ijb/vol4/iss1/20

#### See Also

```
gsMMD, gsMMD.default, gsMMD2.default
```

## **Examples**

```
## Not run:
  library(ALL)
  data(ALL)
  eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]
  mem.str <- as.character(eSet1$BT)</pre>
  nSubjects <- length(mem.str)</pre>
  memSubjects <- rep(0,nSubjects)</pre>
  # B3 coded as 0, T2 coded as 1
  memSubjects[mem.str == "T2"] <- 1</pre>
  myWilcox <-
  function(x, memSubjects, alpha = 0.05)
    xc <- x[memSubjects == 1]
    xn <- x[memSubjects == 0]</pre>
    m <- sum(memSubjects == 1)</pre>
    res <- wilcox.test(x = xc, y = xn, conf.level = 1 - alpha)
    res2 <- c(resp.value, resstatistic - m * (m + 1) / 2)
    names(res2) <- c("p.value", "statistic")</pre>
    return(res2)
  }
  mat <- exprs(eSet1)</pre>
  tmp <- t(apply(mat, 1, myWilcox, memSubjects = memSubjects))</pre>
  colnames(tmp) <- c("p.value", "statistic")</pre>
  memIni <- rep(2, nrow(mat))</pre>
  memIni[tmp[, 1] < 0.05 & tmp[, 2] > 0] <- 1
  memIni[tmp[, 1] < 0.05 & tmp[, 2] < 0] <- 3
  cat("initial gene cluster size>>\n"); print(table(memIni)); cat("\n");
```

gsMMD2.default

Gene selection based on a mixture of marginal distributions

## Description

Gene selection based on the marginal distributions of gene profiles that characterized by a mixture of three-component multivariate distributions. Input is a data matrix. The user needs to provide initial gene cluster membership.

## Usage

```
gsMMD2.default(X,
               memSubjects,
               memIni,
               maxFlag = TRUE,
               thrshPostProb = 0.5,
               geneNames = NULL,
               alpha = 0.05,
               transformFlag = FALSE,
               transformMethod = "boxcox",
               scaleFlag = TRUE,
               criterion = c("cor", "skewness", "kurtosis"),
               minL = -10,
               maxL = 10,
               stepL = 0.1,
               eps = 0.001,
               ITMAX = 100,
               plotFlag = FALSE,
               quiet=TRUE)
```

## **Arguments**

X a data matrix. The rows of the matrix are genes. The columns of the matrix are

subjects.

memSubjects a vector of membership of subjects. memSubjects[i]=1 means the i-th subject

belongs to diseased group, 0 otherwise.

memIni a vector of user-provided gene cluster membership.

maxFlag logical. Indicate how to assign gene class membership. maxFlag=TRUE means

that a gene will be assigned to a class in which the posterior probability of the gene belongs to this class is maximum. maxFlag=FALSE means that a gene

will be assigned to class 1 if the posterior probability of the gene belongs to class 1 is greater than thrshPostProb. Similarly, a gene will be assigned to class 1 if the posterior probability of the gene belongs to class 1 is greater than thrshPostProb. If the posterior probability is less than thrshPostProb, the gene will be assigned to class 2 (non-differentially expressed gene group).

thrshPostProb threshold for posterior probabilities. For example, if the posterior probability

that a gene belongs to cluster 1 given its gene expression levels is larger than

thrshPostProb, then this gene will be assigned to cluster 1.

geneNames an optional character vector of gene names

alpha significant level which is equal to 1-conf.level, conf.level is the argument

for the function t.test.

transformFlag logical. Indicate if data transformation is needed

transformMethod

method for transforming data. Available methods include "boxcox", "log2",

"log10", "log", "none".

scaleFlag logical. Indicate if gene profiles are to be scaled. If transformFlag=TRUE and

scaleFlag=TRUE, then scaling is performed after transformation. To avoid linear dependence of tissue samples after scaling gene profiles, we delete one tissue

sample after scaling (c.f. details).

criterion if transformFlag=TRUE, criterion indicates what criterion to determine if

data looks like normal. "cor" means using Pearson's correlation. The idea is that the observed quantiles after transformation should be close to theoretical normal quantiles. So we can use Pearson's correlation to check if the scatter plot of theoretical normal quantiles versus observed quantiles is a straightline. "skewness" means using skewness measure to check if the distribution of the transformed data are close to normal distribution; "kurtosis" means using kurto-

sis measure to check normality.

minL lower limit for the lambda parameter used in Box-Cox transformation

maxL upper limit for the lambda parameter used in Box-Cox transformation

stepL tolerance when searching the optimal lambda parameter used in Box-Cox trans-

formation

eps a small positive value. If the absolute value of a value is smaller than eps, this

value is regarded as zero.

ITMAX maximum iteration allowed for iterations in the EM algorithm

plotFlag logical. Indicate if the Box-Cox normality plot should be output.

quiet logical. Indicate if intermediate results should be printed out.

#### **Details**

We assume that the distribution of gene expression profiles is a mixture of 3-component multivariate normal distributions  $\sum_{k=1}^3 \pi_k f_k(x|\theta)$ . Each component distribution  $f_k$  corresponds to a gene cluster. The 3 components correspond to 3 gene clusters: (1) up-regulated gene cluster, (2) non-differentially expressed gene cluster, and (3) down-regulated gene cluster. The model parameter vector is  $\theta = (\pi_1, \pi_2, \pi_3, \mu_{c1}, \sigma_{c1}^2, \rho_{c1}, \mu_{n1}, \sigma_{n1}^2, \rho_{n1}, \mu_2, \sigma_2^2, \rho_2, \mu_{c3}, \sigma_{c3}^2, \rho_{c3}, \mu_{n3}, \sigma_{n3}^2, \rho_{n3}$ .

where  $\pi_1$ ,  $\pi_2$ , and  $\pi_3$  are the mixing proportions;  $\mu_{c1}$ ,  $\sigma_{c1}^2$ , and  $\rho_{c1}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 1 (up-regulated genes) for diseased subjects;  $\mu_{n1}$ ,  $\sigma_{n1}^2$ , and  $\rho_{n1}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 1 (up-regulated genes) for non-diseased subjects;  $\mu_2$ ,  $\sigma_2^2$ , and  $\rho_2$  are the marginal mean, variance, and correlation of gene expression levels of cluster 2 (non-differentially expressed genes);  $\mu_{c3}$ ,  $\sigma_{c3}^2$ , and  $\rho_{c3}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for diseased subjects;  $\mu_{n3}$ ,  $\sigma_{n3}^2$ , and  $\rho_{n3}$  are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for non-diseased subjects.

Note that genes in cluster 2 are non-differentially expressed across abnormal and normal tissue samples. Hence there are only 3 parameters for cluster 2.

To make sure the identifiability, we set the following contraints:  $\mu_{c1} > \mu_{n1}$  and  $\mu_{c3} < \mu_{n3}$ .

To make sure the marginal covariance matrices are poisitive definite, we set the following contraints:  $-1/(n_c-1) < \rho_{c1} < 1, -1/(n_n-1) < \rho_{n1} < 1, -1/(n-1) < \rho_2 < 1, -1/(n_c-1) < \rho_{c3} < 1, -1/(n_n-1) < \rho_{n3} < 1.$ 

We also has the following constraints for the mixing proportion:  $\pi_3 = 1 - \pi_1 - \pi_2$ ,  $\pi_k > 0$ , k = 1, 2, 3.

We apply the EM algorithm to estimate the model parameters. We regard the cluster membership of genes as missing values.

To facilitate the estimation of the parameters, we reparametrize the parameter vector as  $\theta^* = (\pi_1, \pi_2, \mu_{c1}, \sigma_{c1}^2, r_{c1}, \delta_{n1}, \sigma_{n1}^2, r_{n1}, \mu_2, \sigma_2^2, r_2, \mu_{c3}, \sigma_{c3}^2, r_{c3}, \delta_{n3}, \sigma_{n3}^2, r_{n3})$ , where  $\mu_{n1} = \mu_{c1} - \exp(\delta_{n1}), \mu_{n3} = \mu_{c3} + \exp(\delta_{n3}), \rho_{c1} = (\exp(r_{c1}) - 1/(n_c - 1))/(1 + \exp(r_{c1})), \rho_{n1} = (\exp(r_{n1}) - 1/(n_n - 1))/(1 + \exp(r_{n1})), \rho_{2} = (\exp(r_2) - 1/(n - 1))/(1 + \exp(r_2)), \rho_{c3} = (\exp(r_{c3}) - 1/(n_c - 1))/(1 + \exp(r_{c3})), \rho_{n3} = (\exp(r_{n3}) - 1/(n_n - 1))/(1 + \exp(r_{n3})).$ 

Given a gene, the expression levels of the gene are assumed independent. However, after scaling, the scaled expression levels of the gene are no longer independent and the rank  $r^* = r - 1$  of the covariance matrix for the scaled gene profile will be one less than the rank r for the un-scaled gene profile Hence the covariance matrix of the gene profile will no longer be positive-definite. To avoid this problem, we delete a tissue sample after scaling since its information has been incorrporated by other scaled tissue samples. We arbitrarily select the tissue sample, which has the biggest label number, from the tissue sample group that has larger size than the other tissue sample group. For example, if there are 6 cancer tissue samples and 10 normal tissue samples, we delete the 10-th normal tissue sample after scaling.

## Value

A list contains 13 elements.

dat the (transformed) microarray data matrix. If tranformation performed, then dat

will be different from the input microarray data matrix.

memSubjects the same as the input memSubjects.

memGenes a vector of cluster membership of genes. 1 means up-regulated gene; 2 means

non-differentially expressed gene; 3 means down-regulated gene.

memGenes2 an variant of the vector of cluster membership of genes. 1 means differentially

expressed gene; 0 means non-differentially expressed gene.

para parameter estimates (c.f. details).

llkh	value of the loglikelihood function.
wiMat	posterior probability that a gene belongs to a cluster given the expression levels of this gene. Column i is for cluster i.
memIni	the initial cluster membership of genes.
paraIni	the parameter estimates based on initial gene cluster membership.
llkhIni	the value of loglikelihood function.
lambda	the parameter used to do Box-Cox transformation
paraRP	parameter estimates for reparametrized parameter vector (c.f. details).
paraIniRP	the parameter estimates for reparametrized parameter vector based on initial gene cluster membership.

#### Note

The speed of the program can be slow for large data sets, however it has been improved using Fortran code.

## Author(s)

Jarrett Morrow <remdj@channing.harvard.edu>, Weiliang Qiu <Weiliang.Qiu@gmail.com>, Wenqing He <whe@stats.uwo.ca>, Xiaogang Wang <stevenw@mathstat.yorku.ca>, Ross Lazarus <ross.lazarus@channing.harvard.edu>

## References

Qiu, W.-L., He, W., Wang, X.-G. and Lazarus, R. (2008). A Marginal Mixture Model for Selecting Differentially Expressed Genes across Two Types of Tissue Samples. *The International Journal of Biostatistics*. 4(1):Article 20. http://www.bepress.com/ijb/vol4/iss1/20

## See Also

```
gsMMD, gsMMD.default, gsMMD2
```

## **Examples**

```
## Not run:
   library(ALL)
   data(ALL)
   eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]
   mat <- exprs(eSet1)

mem.str <- as.character(eSet1$BT)
   nSubjects <- length(mem.str)
   memSubjects <- rep(0, nSubjects)
# B3 coded as 0, T2 coded as 1
   memSubjects[mem.str == "T2"] <- 1

myWilcox <-
function(x, memSubjects, alpha = 0.05)
{</pre>
```

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```
xc <- x[memSubjects == 1]
      xn <- x[memSubjects == 0]</pre>
      m <- sum(memSubjects == 1)</pre>
      res <- wilcox.test(x = xc, y = xn, conf.level = 1 - alpha)
      res2 <- c(resp.value, resstatistic - m * (m + 1) / 2)
      names(res2) <- c("p.value", "statistic")</pre>
      return(res2)
    }
    tmp <- t(apply(mat, 1, myWilcox, memSubjects = memSubjects))</pre>
    colnames(tmp) <- c("p.value", "statistic")</pre>
   memIni <- rep(2, nrow(mat))</pre>
   memIni[tmp[, 1] < 0.05 \& tmp[, 2] > 0] <- 1
   memIni[tmp[, 1] < 0.05 \& tmp[,2] < 0] <- 3
   cat("initial gene cluster size>>\n"); print(table(memIni)); cat("\n");
    obj.gsMMD <- gsMMD2.default(mat, memSubjects, memIni = memIni,</pre>
            transformFlag = TRUE, transformMethod = "boxcox", scaleFlag = TRUE)
    round(obj.gsMMD$para, 3)
## End(Not run)
```

obtainResi

Replace expression levels by the residuals of regression analysis to remove the confounding effects.

## Description

Replace expression levels by the residuals of regression analysis in which predictor of interest is not in the regression model. The purpose of this function is to remove potential confounding factors.

## Usage

```
obtainResi(es, fmla)
```

### **Arguments**

es

An ExpressionSet object.

fmla

A formula object that specifies the covariates of the linear regression model. The variable of interest should not be included. No response variable should be specified in fmla since the response variable is always the expression level. See function lmFit of R Bioconductor package limma.

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#### **Details**

To remove confounding effects, we can replace the expression level by the residuals of a linear regression model with response variable the expression level and covariates the potential confounders. The functions lmFit and eBayes will be used to obtain regression coefficients.

#### Value

An ExpressionSet object with expression levels replaced by residuals of linear regression analysis.

#### Note

The number of arrays of the returned ExpressionSet object might be smaller than that of the original ExpressionSet object, due to missing values in covariates.

### Author(s)

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plotHistDensity

Plot of histogram and density estimate of the pooled gene expression levels.

#### **Description**

Plot of histogram of pooled gene expression levels, composited with density estimate based on the mixture of marginal distributions. The density estimate is based on the assumption that the marginal correlations between subjects are zero.

## Usage

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### **Arguments**

obj.gsMMD an object returned by gsMMD.default, gsMMD2, or gsMMD2.default

plotFlag logical. Indicate the plot will based on which type of subjects.

plotComponent logical. Indicate if components of the mixture of marginal distribution will be

plotted.

myxlab label for x-axis myylab label for y-axis mytitle title of the plot

x.legend the x-corrdiates of the legend y.legend the y-corrdiates of the legend

numPoints logical. Indicate how many genes will be plots.

mycol color for the density estimates (overall and components)
mylty line styles for the density estimates (overall and components)
mylwd line width for the density estimates (overall and components)

cex.main font for main title

cex.lab font for x- and y-axis labels cex.axis font for x- and y-axis

cex font for texts

bty the type of box to be drawn around the legend. The allowed values are "o" and

"n" (the default).

## Details

For a given type of subjects, we pool their expression levels together if the marginal correlations among subjects are zero. We then draw a histogram of the pooled expression levels. Next, we composite density estimates of gene expression levels for the overal distribution and the 3 component distributions.

## Value

y3

A list containing coordinates of the density estimates:

Χ	sorted pooled gene expression levels for cases or controls.
x2	a subset of x specified by the sequence: $seq(from = 1, to = len.x, by = delta)$ , where $len.x$ is the length of the vector x, and $delta = floor(len.x/numpoints)$ .
у	density estimate corresponding to x2
y1	weighted density estimate for gene cluster 1
y2	weighted density estimate for gene cluster 2

weighted density estimate for gene cluster 3

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#### Note

The density estimate is obtained based on the assumption that the marginal correlation among subjects is zero. If the estimated marginal correlation obtained by gsMMD is far from zero, then do not use this plot function.

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#### References

Qiu, W.-L., He, W., Wang, X.-G. and Lazarus, R. (2008). A Marginal Mixture Model for Selecting Differentially Expressed Genes across Two Types of Tissue Samples. *The International Journal of Biostatistics*. 4(1):Article 20. http://www.bepress.com/ijb/vol4/iss1/20

## **Examples**

```
## Not run:
library(ALL)
data(ALL)
eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]
mem.str <- as.character(eSet1$BT)</pre>
nSubjects <- length(mem.str)</pre>
memSubjects <- rep(0,nSubjects)</pre>
# B3 coded as 0 (control), T2 coded as 1 (case)
memSubjects[mem.str == "T2"] <- 1</pre>
obj.gsMMD <- gsMMD(eSet1, memSubjects, transformFlag = TRUE,
  transformMethod = "boxcox", scaleFlag = TRUE, quiet = FALSE)
plotHistDensity(obj.gsMMD, plotFlag = "case",
    mytitle = "Histogram of for T2 imposed with estimated density (case)",
   plotComponent = TRUE,
    x.legend = c(0.8, 3),
    y.legend = c(0.3, 0.4),
    numPoints = 500)
## End(Not run)
```

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