

A tutorial for the Bioconductor package **hierGWAS**

Laura Buzdugan

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1 Introduction

hierGWAS tests statistical significance in Genome Wide Association Studies (GWAS), using a joint model of all SNPs. This leads to a stronger interpretation of single, or groups of SNPs compared to the marginal approach. The method provides an asymptotic control of the Family Wise Error Rate (FWER), as well as an automatic, data-driven refinement of the SNP clusters to smaller groups or single markers [1].

The method can be used for case-control studies, as well as for continuous trait studies. Additionally, one can control for one or more covariates.

1.1 Model

The two components of the model are the genotype X and the phenotype Y . Y is a vector of length n , where n represents the number of samples (e.g. subjects). Y_i , the phenotype corresponding to

person i , can encode either the disease status (0 or 1), or the continuous value of a trait. X is a matrix of size $n \times p$, where p is the number of SNPs to be analyzed. $X_{i,j}$ encodes the number of minor alleles of the j th SNP for person i , thus it can take values 0, 1, 2.

The genotype-phenotype relationship is expressed using a generalized linear model [2]. If the phenotype is continuous, this translates to a linear model:

$$Y_i = \beta_0 + \sum_{j=1}^p \beta_j X_{i,j} + \epsilon_i \quad (i = 1, \dots, n)$$

where $\epsilon_i, \dots, \epsilon_n$ are independent and identically distributed error terms with expectation 0. If the phenotype is binary, representing case (=1) or control (=0) status, we use a logistic regression model:

$$\pi_i = P(Y_i = 1 | X_i, \beta) = \frac{\exp(\eta_i)}{1 + \exp(\eta_i)} \quad (i = 1, \dots, n)$$

$$\ln \frac{\pi_i}{1 - \pi_i} = \eta_i = \beta_0 + \sum_{j=1}^p \beta_j X_{i,j}$$

where π represents the probability of a subject having case status, given its SNPs X_i .

In both models β_0 represents the intercept and β_j are the (logistic) regression coefficients which quantify the association between the response and SNP j .

Our goal is to assess the statistical significance of single SNPs, or groups of correlated SNPs, with respect to the phenotype. This has to be made precise: we aim for p-values, adjusted for multiple testing, when testing the hypotheses: for single SNP j

$$H_{0,j} : \beta_j = 0 \text{ versus } H_{A,j} : \beta_j \neq 0, \quad (1)$$

or for a group $G \subseteq \{1, \dots, p\}$ of SNPs

$$H_{0,G} : \beta_j = 0 \text{ for all } j \in G$$

$$\text{versus } H_{A,G} : \text{at least for one } j \in G \text{ we have that } \beta_j \neq 0. \quad (2)$$

The obtained p-values are with respect to a regression model and hence, they share the interpretation with the regression parameters described above.

1.2 Workflow

The entire procedure for hierarchical inference is schematically summarized in Figure 1. Preprocessing refers to the steps taken to clean the data, by removing SNPs, samples. This should be performed before starting the analysis. The three stages of the procedure are described in detail in sections 3.1, 3.2 and 3.3.

2 Preparing Data

2.1 Data Formats

The two required variables in order to perform the analysis are the phenotype and genotype data. The genotype data, \mathbf{x} , should be a matrix of size $\mathbf{n} \times \mathbf{p}$, where \mathbf{n} represents the number of samples (subjects), and \mathbf{p} the number of SNPs. The SNPs must be coded numerically (0,1,2 copies of a specific allele). The phenotype data, \mathbf{y} should be a vector of length \mathbf{n} , and it should have either binary (0,1), or continuous valued elements.

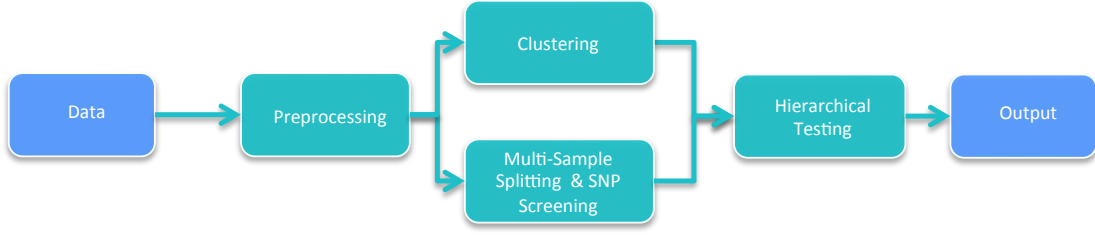


Figure 1: Flowchart of the method.

If one is working with PLINK, these two data structures can easily be created in R after the PLINK data file is read.

There are two optional input variables. `SNP_index`, a vector of length p , assigns a label to each SNP. These could represent chromosomes, or some other grouping of the SNPs. `covar`, either of vector of length n , or a matrix of size $n \times c$, stores the covariates one wishes to control for.

2.2 Missingness

In general, even after preprocessing, SNP data contains missing values. While this is not an issue in a marginal analysis, where missing data are omitted, multivariate methods such as `lm`, `glm`, do not allow for data with missingness.

Thus, one must impute these missing values before starting the analysis. There are several different methods to do this, either in R, after the data is imported, or before. If done inside R, one can choose from packages such as `mice`, `mi` or `missforest`, which perform multiple imputation.

If one wishes to use methods tailored for GWAS data, software such as `SHAPEIT` [3] can be employed. Although the goal of `SHAPEIT` is to impute additional SNPs that were not genotyped, it will also impute the missing values for the genotyped SNPs. This is done in the process of phasing the chromosomes, when missing values are already imputed.

2.3 Toy Data

Given the usual size of GWAS data, performing the analysis on a real dataset with $> 10^5$ SNPs is computationally expensive. For this reason, in order to illustrate the method, we generated a small toy dataset using PLINK.

The data contains $n = 500$ samples (250 cases, 250 controls) and $p = 1000$ SNPs. Out of these 1000 SNPs, 990 have no association with the phenotype, while the remaining 10 have a population odds ratio of 2. The SNPs were binned into different allele frequency ranges, to create a more realistic example.

The SNPs are separated into two chromosomes: the first half of the SNPs are from chromosome 1, while the second half from chromosome 2. Finally, there are two control variables: sex (0 for males, 1 for females) and age (between 18 and 65).

The data structure, entitled `simGWAS`, has the following components:

- `SNP.1`: The first SNP, of dimension 500×1 . Each row represents a subject.
- ...

- SNP.1000: The last SNP, of dimension 500×1 . Each row represents a subject.
- y: The response vector. It can be continuous or discrete.
- sex: The first covariate, representing the sex of the subjects: 0 for men and 1 for women.
- age: The second covariate, representing the age of the subjects.

3 Data Analysis

The `hierGWAS` R-package contains the following functions:

Function	Description
<code>cluster.snp</code>	clusters the SNP hierarchically
<code>multisplit</code>	performs the multiple sample splitting and LASSO regression
<code>test.hierarchy</code>	hierarchically tests the SNPs
<code>compute.r2</code>	computes the r^2 for a group of SNPs

The first three functions perform the clustering, regression and testing. The outputs of `cluster.snp` and `multisplit` are required as inputs for `test.hierarchy`, so these two functions need to be executed before the third one. On the other hand, `cluster.snp` and `multisplit` are independent, so they can be run in any order. In order to speed up the computations, one should consider running them in parallel if the resources allow it. The last function, `compute.r2`, allows the user to calculate the variance explained by any group of SNPs of arbitrary size.

```
> library(hierGWAS)
> data(simGWAS)
> sim.geno <- data.matrix(simGWAS[,1:1000])
> sim.pheno <- simGWAS$y
> sim.covar <- cbind(simGWAS$sex, simGWAS$age)
```

In the following we will describe each of the four functions, and show how they should be used.

3.1 Hierarchical Clustering of SNPs

The first step is to hierarchically cluster the SNPs. `cluster.snp` uses the `hclust` function from R, but provides a different distance measure. Hierarchical clustering is a computationally intensive procedure, and for large datasets it becomes unfeasible. For this reason, one can divide the SNPs into non-overlapping sets, and cluster each set separately. One natural division is the grouping of SNPs into distinct chromosomes, but the user is free to define alternative divisions.

In the case of our toy data, the SNPs belong to either chromosome 1 or 2, so we cluster them into two distinct hierarchies, by specifying the indices of the SNPs which come from either chromosome 1 or 2. Note that in this case, due to the small size of the data, it would be equally feasible to cluster all the SNPs into a single tree.

```
> # cluster SNPs in chromosome 1
> SNPindex.chrom1 <- seq(1,500)
> dendr.chrom1 <- cluster.snp(sim.geno, SNP_index = SNPindex.chrom1)
> # cluster SNPs in chromosome 2
> SNPindex.chrom2 <- seq(501,1000)
> dendr.chrom2 <- cluster.snp(sim.geno, SNP_index = SNPindex.chrom2)
```

The inputs for `cluster.snp` are `x`, the genotype matrix, respectively `SNPindex.chrom1` and `SNPindex.chrom2`, the indices of SNPs in chromosomes 1 and 2. `x` was used to compute the dissimilarity measure between the SNPs.

The default dissimilarity measure between two SNPs is $1 - \text{LD}$ (Linkage Disequilibrium), where LD is defined as the square of the Pearson correlation coefficient. If the user wishes to use a different dissimilarity measure, this will then be the sole input to `cluster.snp`. For example, if we were to use a different measure, the input would have been only the dissimilarity matrix. Thus, for our toy data, we would have had to provide either two 500×500 matrices, one per chromosome, and execute the function separately for each chromosome, or give one 1000×1000 dissimilarity matrix for the entire dataset.

Finally, the default agglomeration method is average linkage, however the user can choose between multiple methods implemented by `hclust`.

For large datasets, one can speed up the analysis by running the clustering of separate chromosomes in parallel. This can be done using the `parallel` R package.

3.2 Multiple Sample Splitting and LASSO Regression

The second step, which can be run independently from the first one, is to do repeated LASSO regressions on random sample splits. This part of the analysis is implemented in the `multisplit` function. This function takes as input the genotype and phenotype data, as well as one or more covariates.

The procedure is as follows:

1. Randomly split the sample into two equal parts: I_1 and I_2
2. Do LASSO selection on the data from I_1 . Save the $n/6$ selected SNPs.
3. Repeat steps 1-2 B times. The default value for B is 50, but a different number of random splits can be specified.

The output of this function is a list with two components:

- `out.sample`: a matrix of size $B \times [n/2]$ containing the second subsample (I_2) for each split.
- `sel.coeff`: a matrix of size $B \times [n/6]$ containing the selected variables in each split.

For our example, the code is the following:

```
> res.multisplit <- multisplit(sim.geno,sim.pheno,covar = sim.covar)
> # the matrix of selected coefficients for each sample split
> show(res.multisplit$sel.coeff[1:10,1:10])
```

	[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]	[,10]
[1,]	995	990	991	989	996	585	709	846	956	620
[2,]	991	995	990	859	997	348	897	299	888	989
[3,]	991	995	990	992	996	588	989	848	149	89
[4,]	995	990	991	989	801	492	315	859	129	546
[5,]	995	991	992	990	989	906	641	377	996	276
[6,]	991	995	992	209	304	846	990	597	730	843
[7,]	990	991	995	625	730	992	655	989	996	156
[8,]	989	995	990	846	891	991	996	218	992	997
[9,]	991	995	992	218	223	997	990	473	159	989
[10,]	991	995	990	996	989	992	976	845	998	120

```
> # the samples which will be used for testing
> show(res.multisplit$out.sample[1:10,1:10])
```

	[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]	[,10]
[1,]	1	4	8	13	14	15	20	22	23	24
[2,]	1	3	6	8	9	10	11	12	17	19
[3,]	1	2	3	4	5	7	11	13	16	20
[4,]	3	4	5	7	14	16	18	19	21	25
[5,]	4	7	11	12	17	20	21	30	33	34
[6,]	6	7	8	9	12	13	17	18	19	21
[7,]	1	2	3	10	14	15	16	17	18	19
[8,]	1	5	7	8	10	15	16	17	18	21
[9,]	1	2	3	5	7	8	9	11	12	15
[10,]	4	7	12	13	18	19	22	23	31	33

3.3 Hierarchical Testing of SNPs

The last step of the procedure is the hierarchical testing of SNPs. We describe the steps for the toy data:

1. Test the global hypothesis $H_{0,G_{\text{global}}}$ where $G_{\text{global}} = \{1, \dots, p\}$: that is, we test whether all SNPs have corresponding (generalized) regression coefficients equal to zero or alternatively, whether there is at least one SNP which has a non-zero regression coefficient. If we can reject this global hypothesis, we go to the next step.
2. Test the hypotheses $H_{0,G_1}, \dots, H_{0,G_2}$ where G_k contains all the SNPs from chromosome k . For those chromosomes k where H_{0,G_k} can be rejected, we go to the next step.
3. Test hierarchically the groups G which correspond to chromosomes k where H_{0,G_k} is rejected: first consider the largest groups and then proceed hierarchically (down the cluster tree) to smaller groups until a hypothesis $H_{0,G}$ can not be rejected anymore or the level of single SNPs is reached.
4. The output is a collection of groups $G_{\text{final},1}, \dots, G_{\text{final},m}$ where $H_{0,G_{\text{final},k}}$ is rejected ($k = 1, \dots, m$) and all subgroups of $G_{\text{final},k}$ ($k = 1, \dots, m$) downwards in the cluster tree are not significant anymore.

With this procedure, one needs to do the hypothesis tests in such a hierarchical procedure at certain levels to guarantee that the familywise error, i.e., the probability for at least one false rejection of the hypotheses among the multiple tests, is smaller or equal to α for some pre-specified $0 < \alpha < 1$, e.g., $\alpha = 0.05$.

For our dataset, the `test.hierarchy` function takes as input the following variables:

- x: the genotype matrix
- y: the phenotype vector
- dendr: the hierarchical tree (of one of the chromosomes)
- res.multisplit: the output of the LASSO regression
- SNP_index: the indices of SNPs (in one of the chromosomes)
- global.test: specifies whether the global null hypothesis should be tested
- verbose: reports information on progress

We then run the function for both chromosomes 1 and 2.

```
> result.chrom1 <- test.hierarchy(sim.geno, sim.pheno, dendr.chrom1, res.multisplit,
+                               covar = sim.covar, SNP_index = SNPindex.chrom1)
> result.chrom2 <- test.hierarchy(sim.geno, sim.pheno, dendr.chrom1, res.multisplit,
+                               covar = sim.covar, SNP_index = SNPindex.chrom2,
+                               global.test = FALSE, verbose = FALSE)
> show(result.chrom2)
```

```
[[1]]
[[1]]$label
 [1] 851 919 506 613 557 585 704 717 911 951 760 569 581 763 908
[16] 896 886 977 502 622 568 942 671 804 612 610 579 854 515 537
[31] 586 927 528 549 597 735 814 593 750 647 783 878 628 918 819
[46] 548 781 544 840 565 601 588 752 773 516 736 957 959 564 952
[61] 895 780 985 580 917 521 606 734 809 984 578 898 640 682 535
[76] 806 842 646 1000 584 958 599 936 835 967 678 726 602 639 724
[91] 796 527 686 694 866 903 594 887 555 980 636 978 779 940 688
[106] 893 501 948 587 897 650 954 784 631 730 623 648 653 869 966
[121] 765 975 638 681 624 540 856 689 680 997 643 605 943 922 723
[136] 970 615 670 591 659 772 955 667 912 577 652 890 864 899 712
[151] 793 981 609 916 654 709 664 845 630 720 838 920
```

```
[[1]]$pval
[1] 0.04812043
```

```
[[2]]
[[2]]$label
 [1] 963 813 871 929 748 849 844 995 553 729 830 982 771 841 900 541 932 695 762
[20] 529 850 530 823 611 700 665 843 973 663 811 619 789 562 675 998 803 744 798
```

```
[[2]]$pval
[1] 0.04211383
```

```
[[3]]
[[3]]$label
[1] 992
```

```
[[3]]$pval
[1] 0.009781007
```

```
[[4]]
[[4]]$label
[1] 991
```

```
[[4]]$pval
[1] 0.02435146
```

The output of `test.hierarchy` is a list containing groups or individually significant SNPs, as well as their p-values.

Based on the indices of the significant SNPs, one can go back to the original data and retrieve the SNP rsIDs.

Due to the fact that the procedure begins with testing the global null $H_{0,G_{\text{global}}}$, if we subdivide the SNPs into chromosomes or other groups, we will end up testing the global null for each division. In order to save time, once the global null has been rejected (e.g. for chromosome 1), when testing chromosome 2, the `test.global` parameter should be set to `FALSE`, to avoid retesting the null.

The final parameter of the function, `verbose`, offers the user updates about the progress of the algorithm. By default this parameter is set to `TRUE`, but the messages can be suppressed by setting it to `FALSE`.

3.4 Computation of explained variance

One has the option of calculating the variance explained by any group of SNPs, using the `compute.r2` function. The inputs are:

- `x`: the genotype matrix
- `y`: the phenotype vector
- `res.multisplit`: the output of the LASSO regression
- `covar`: the matrix of covariates
- `SNP_index`: the indices of SNPs whose r^2 will be computed

The r^2 of a group is computed in the following way:

1. Intersect the group indices with those of the selected coefficients in split b
2. Compute the r^2 of the model with SNPs from point 1.
3. Repeat steps 1-2 B times. The final r^2 is the mean of the B r^2 values.

For our toy data, given that we know a-priori that the last 10 SNPs are the ones that increase the risk of disease, we chose to compute the variance explained jointly by them. This is done using the following command:

```
> SNP_index <- seq(991,1000)
> res.r2 <- compute.r2(sim.geno, sim.pheno, res.multisplit, covar = sim.covar, SNP_index = SNP_index)
> show(res.r2)

[1] 0.2467755
```

4 Session Info

```
> sessionInfo()

R version 4.0.3 (2020-10-10)
Platform: x86_64-apple-darwin17.0 (64-bit)
Running under: macOS Mojave 10.14.6

Matrix products: default
BLAS: /Library/Frameworks/R.framework/Versions/4.0/Resources/lib/libRblas.dylib
```

LAPACK: /Library/Frameworks/R.framework/Versions/4.0/Resources/lib/libRlapack.dylib

locale:

[1] C/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8

attached base packages:

[1] stats graphics grDevices utils datasets methods base

other attached packages:

[1] hierGWAS_1.20.0

loaded via a namespace (and not attached):

[1] compiler_4.0.3 Matrix_1.2-18 tools_4.0.3 survival_3.2-7
[5] splines_4.0.3 codetools_0.2-16 grid_4.0.3 iterators_1.0.13
[9] foreach_1.5.1 fmsb_0.7.0 fastcluster_1.1.25 shape_1.4.5
[13] glmnet_4.0-2 lattice_0.20-41

References

- [1] L. Buzdugan et al. *Assessing statistical significance in predictive genome-wide association studies*. (unpublished).
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